

$$8) y = \frac{1}{x^8} = x^{-8}$$

$$y' = -8x^{-9}$$

$$y' = \frac{-8}{x^9}$$

$$28) y = \frac{\pi}{(3x)^2} = \frac{\pi}{9x^2}$$

$$y = \frac{\pi}{9}x^{-2}$$

$$y' = \frac{\pi}{9}(-2x^{-3})$$

$$y' = \frac{-2\pi}{9x^3}$$

$$46) y = 3x(6x - 5x^2)$$

$$y = 18x^2 - 15x^3$$

$$y' = 36x - 45x^2$$

$$48) y = \frac{\sec x}{x}$$

$$y' = \frac{(\sec x \cdot \tan x)(x) - (\sec x)(1)}{(x)^2}$$

$$y' = \frac{\sec x (x \tan x - 1)}{x^2}$$

64) Equation of tangent line:

$$f(x) = (x-1)(x^2-2), (0, 2)$$

$$f'(x) = (1)(x^2-2) + (x-1)(2x)$$

$$f'(x) = x^2 - 2 + 2x^2 - 2x$$

$$f'(x) = 3x^2 - 2x - 2$$

$$f'(0) = 3(0)^2 - 2(0) - 2 = -2$$

$$y - 2 = -2(x - 0)$$

$$\text{or } y = -2x + 2$$

$$f(x) = x^3 - 2x - x^2 + 2$$

$$f'(x) = 3x^2 - 2 - 2x$$

2.3 practice

74) Where horizontal tangent line?

$$f(x) = \frac{x^2}{x^2 + 1}$$

$$f'(x) = \frac{(2x)(x^2+1) - (x^2)(2x)}{(x^2+1)^2}$$

$$2x^3 + 2x - 2x^3$$

$$\frac{2x}{(x^2+1)^2} = 0$$

$$2x = 0$$

$$x = 0$$

94) $f(x) = x + 32x^{-2}$, find $f''(x)$

$$f'(x) = 1 - 64x^{-3} \quad \begin{matrix} / \\ 64 \end{matrix}$$

$$f''(x) = 192x^{-4} \quad \begin{matrix} / \\ 192 \\ x^3 \end{matrix}$$

$$f''(x) = \frac{192}{x^4}$$

$$10) f(x) = (9x+2)^{\frac{2}{3}}$$

$$f'(x) = \frac{2}{3} (9x+2)^{-\frac{1}{3}} (9)$$

$$f'(x) = \frac{6}{(9x+2)^{\frac{1}{3}}}$$

$$24) f(x) = x(3x-9)^3$$

$$f'(x) = \underline{1(3x-9)^3} + \underline{x(3(3x-9)^2(3))}$$

$$f'(x) = (3x-9)^2 (\underline{3x-9} + \underline{9x})$$

$$(3x-9)^2 (12x-9)$$

$$f'(x) = 3(3x-9)^2 (4x-3)$$

$$28) y = \frac{x}{\sqrt{x^4+4}} \quad (x^4+4)^{\frac{1}{2}}$$

$$y' = \frac{(1)\sqrt{x^4+4} - x\left(\frac{1}{2}(x^4+4)^{-\frac{1}{2}}(4x^3)\right)}{(\sqrt{x^4+4})^2}$$

$$y' = \frac{\sqrt{x^4+4}}{1} \cdot \frac{(x^4+4)^{\frac{1}{2}}}{(x^4+4)^{\frac{1}{2}}} - \frac{2x^4}{(x^4+4)^{\frac{1}{2}}}$$

$$y' = \frac{x^4+4 - 2x^4}{(x^4+4)^{\frac{1}{2}}}$$

$$y' = \frac{4-x^4}{(x^4+4)^{\frac{3}{2}}}$$

$$54) h(t) = 2 \cot^2(\pi t + 2)$$

$$h(t) = 2(\cot(\pi t + 2))^2$$

$$h'(t) = 4(\cot(\pi t + 2))'$$

$$\rightarrow (-\csc^2(\pi t + 2))(\pi)$$

$$h'(t) = -4\pi \cot(\pi t + 2) \csc^2(\pi t + 2)$$

72) Equation of tangent line:

$$y = \cos(3x), \left(\begin{array}{c} \pi/4 \\ x \end{array}, \begin{array}{c} -\sqrt{2}/2 \\ y \end{array} \right)$$

$$y' = -\sin(3x)(3)$$

$$y' = -3\sin(3x)$$

$$y' = -3\sin\left(\frac{3\pi}{4}\right) = -\frac{3\sqrt{2}}{2}$$

$$y + \frac{\sqrt{2}}{2} = -\frac{3\sqrt{2}}{2}\left(x - \frac{\pi}{4}\right)$$

84) $f(x) = \frac{1}{x-2}$, find $f''(x)$

$$f(x) = (x-2)^{-1}$$

$$f'(x) = -1(x-2)^{-2} \quad (1)$$

$$f''(x) = 2(x-2)^{-3}$$

$$f''(x) = \frac{2}{(x-2)^3}$$

$$8) \sqrt{xy} = x - 2y \quad (xy)^{\frac{1}{2}} = x - 2y$$

$$\frac{1}{2}(xy)^{-\frac{1}{2}}(1 \cdot y + x \cdot y') = 1 - 2y'$$

$$\frac{1}{2}(xy)^{-\frac{1}{2}}y + \frac{1}{2}(xy)^{-\frac{1}{2}}(xy') = 1 - 2y'$$

$$\frac{y}{2(xy)^{\frac{1}{2}}} + 2y' = \frac{-y}{2(xy)^{\frac{1}{2}}} + 1$$

$$y' \left(\frac{x}{2\sqrt{xy}} + 2 \right) = \frac{-y}{2\sqrt{xy}} + 1 \cdot \frac{2\sqrt{xy}}{2\sqrt{xy}}$$

$$\frac{x}{2\sqrt{xy}} + 2 \quad \frac{x}{2\sqrt{xy}} + 2 \cdot \frac{2\sqrt{xy}}{2\sqrt{xy}}$$

$$y' = \frac{-y + 2\sqrt{xy}}{2\sqrt{xy}}$$

$$\frac{x + 4\sqrt{xy}}{2\sqrt{xy}}$$

$$y' = \frac{2\sqrt{xy} - y}{x + 4\sqrt{xy}}$$

$$28) x \cos y = 1, \quad \left(2, \frac{\pi}{3}\right)$$

$$1 \cos y + x(-\sin y)y' = 0$$

$$\cos\left(\frac{\pi}{3}\right) + 2 \sin\left(\frac{\pi}{3}\right)y' = 0$$

$$\frac{1}{2} - 2\left(\frac{\sqrt{3}}{2}\right)y' = 0$$

$$\frac{-\sqrt{3}}{-\sqrt{3}} y' = \frac{-\frac{1}{2}}{-\sqrt{3}}$$

$$y' = \frac{1}{2\sqrt{3}} \quad \text{or} \quad \frac{\sqrt{3}}{\sqrt{3}}$$

$$y' = \frac{\sqrt{3}}{6}$$

48) $1 - xy = x - y$, find y''

$$0 - (1 \cdot y + xy') = 1 - y'$$

$$-1y - xy' = 1 - y'$$

$$y' - xy' = 1 + y$$

$$\frac{y'(1-x)}{1-x} = \frac{y+1}{1-x}$$

$$y' = \frac{y+1}{1-x}$$

$$y'' = \frac{(y')(1-x) - (y+1)(-1)}{(1-x)^2}$$

$$y'' = \frac{\left(\frac{y+1}{1-x}\right)(1-x) + y+1}{(1-x)^2}$$

$$y'' = \frac{2y+2}{(1-x)^2} \text{ or } \frac{2(y+1)}{(1-x)^2}$$

2) $x^2 + y^2 = 25$ Find $\frac{dy}{dt}$ when $x = 3, y = 4$: Given $\frac{dx}{dt} = 8$

$$2x \frac{dx}{dt} + 2y \frac{dy}{dt} = 0$$

$$2(3)(8) + 2(4) \frac{dy}{dt} = 0$$

-48 8 -48

$$\frac{8 \frac{dy}{dt}}{8} = \frac{-48}{8}$$

$$\frac{dy}{dt} = -6$$

16) Area of a circle changing in respect to time.

$$A = \pi r^2 \quad \frac{dA}{dt} = \pi(2r) \frac{dr}{dt}$$

22) Find rate of change of the volume if $\frac{dr}{dt} = 2$ and $h = 3r$ when $r = 6$

$$V = \frac{1}{3} \pi r^2 h$$



$$V = \frac{1}{3} \pi r^2 (3r) \quad V = \pi r^3$$

$$\frac{dV}{dt} = \pi (3r^2) \frac{dr}{dt}$$

$$\frac{dV}{dt} = \pi (3(6)^2) (2)$$

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$$\frac{dV}{dt} = 216\pi$$